

Comparative study of Sugarcane Bagasse Pyrolysis Methods on Phosphate Ion Adsorption Efficiency: Optimization with BBD-RSM

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Abstract

Utilization of sugarcane bagasse waste as an adsorbent because it has a high silica content, is environmentally friendly, and has a high surface area. Sugarcane bagasse is used as an adsorbent with oxygen pyrolysis (SB@PO) and N₂ (SB@PN) methods, both of which are applied to reduce phosphate waste in water. The adsorption method was chosen to reduce phosphate levels in wastewater. Adsorption parameters include adsorbent mass, contact time, and initial concentration of phosphate solution. Response Surface Methodology (RSM) and Box-Behnken design (BBD) methods are used to optimize the process. Phosphate levels are measured using Differential Pulse Voltammetry (DPV). The characterizations carried out include: FTIR, XRD, FESEM-EDX, and N₂ adsorption-desorption. SB@PO obtained material with a crystalline structure and rich in silica while SB@PN obtained material rich in carbon and amorphous structure. The adsorption optimization results showed that SB@PO was superior to SB@PN, namely the percentage removal and adsorption capacity were 95.97% and 43.48 mg/g for SB@PO, while SB@PN was optimal with the percentage removal and adsorption capacity of 65.75% and 2.2×10^{-4} mg/g, respectively.

Keywords: Adsorption, Waste, Sugarcane bagasse, Phosphate, Pyrolysis, Differential Pulse Voltammetry (DPV), Response Surface Methodology (RSM).

Introduction

Sugarcane bagasse is an organic and environmentally friendly waste, but its combustion can be harmful to human health and cause air pollution. Bagasse is obtained from the processing of sugarcane into sugar. Recycled bagasse is usually used as a raw material for making fertilizer [1], electrodes [2], and adsorbents [3]. Sugarcane bagasse contains cellulose (33.5%); hemicellulose (43.6%); silica (9.35%), and lignin [4]. Based on Sarkar *et al.* [5], it shows that sugarcane bagasse contains SiO₂ (50% - 97%), CaO (1% - 2%), Fe₂O₃ (3% - 4%), MgO (0.5% - 1%), and K₂O (4.2% - 4.4%). Due to its high content, bagasse is processed into products with high sales value, abundant availability, affordability, and environmental friendliness. Bagasse has a high surface area and

adsorption capacity. These properties make it suitable for use as an adsorbent [4].

The processing of sugarcane bagasse into adsorbents has been studied, among others, as biochar [6], silica [7], activated carbon [4], composites [2], and coagulants [8]. The processing of sugarcane bagasse into biochar by pyrolysis method was chosen because it can decompose organic materials using high temperatures without oxygen and with little oxygen. Sugarcane bagasse was pyrolyzed with variations in N₂ and oxygen atmospheres to obtain adsorbents with different characteristics, where when pyrolysis using N₂ atmosphere obtained carbon while oxygen pyrolysis obtained higher silica [9,10]. Thus, in this study, sugarcane bagasse was used as an adsorbent for phosphate adsorption with variations in oxygen and N₂

atmospheric pyrolysis methods to obtain higher silica (SB@PO) and carbon (SB@PN) materials.

Phosphate is a hazardous waste and a major chemical species in the agricultural world, especially in fertilizer production. Fertilizers containing phosphate include: NPK fertilizer, TSP fertilizer, MKP (Mono Potassium Phosphate) fertilizer, SP-36 fertilizer. The need for phosphate fertilizer in Indonesia is increasing and has an impact on the amount of phosphate contaminant waste. In addition, the importance of formulating phosphate fertilizer application on agricultural land so that fertilizer is optimally absorbed by the soil [11]. Excessive application of phosphate fertilizers results in fertilizers not being absorbed with high concentrations flowing from agricultural land to the water system, which causes eutrophication that can kill other organisms [12]. Therefore, processing is carried out to remove high concentrations of phosphate content (M) that are not absorbed in water bodies with 3R (Reduce, Reuse, and Recycle), namely reducing the amount of waste by reducing phosphate fertilizer consumption, reusing excess phosphate fertilizer that can still be used, and reducing the amount of waste disposed of in landfills (TPA).

Several methods have been used to remove phosphate, including biologically coupled induced crystallization [13], adsorption [14,15], sedimentation [16], and electrocoagulation [17]. The adsorption method was chosen because it is simple, low-cost, and more effective at reducing phosphate levels.

Adsorption process parameters include contact time, adsorbent mass, and initial solution concentration [18]. Optimizing phosphate adsorption parameters using the classical approach is inefficient. Besides being time-consuming and labor-intensive, the classical approach also requires a large amount of chemicals [19]. The solution is to use a non-classical approach or experimental design, namely Response Surface Methodology (RSM) with a Box-Behnken design. Experimental design is used to obtain optimum conditions with a small number of trials (runs), thus requiring fewer chemicals and being economical. The Box-Behnken design is the input of the experimental design, which uses 3 levels: The lowest value (-1), the middle value (0), and the highest value (+1) [20]. The Response Surface Methodology (RSM) is the output of the experimental design, which produces the optimum

area of interaction or combination of factors and levels used [21].

Concentration measurement during adsorption using the voltammetric method, namely Differential Pulse Voltammetry (DPV), has advantages in the phosphate measurement process, such as the absence of additional complexing agents, high sensitivity and selectivity. Therefore, in this study, phosphate adsorption measurements were conducted using Differential Pulse Voltammetry (DPV) with graphite as the working electrode, Pt as the auxiliary electrode, and Ag/AgCl as the reference electrode [22].

The novelty of this research lies in the measurement of phosphate ion concentration using the differential pulse voltammetry (DPV) method, because in general the determination of phosphate levels using a UV-Vis Spectrophotometer [23] and the use of DPV has been widely used to determine heavy metal levels [22], but no one has done it for determining phosphate levels. Based on the background description above, this study aims to determine the optimization parameters that influence phosphate adsorption with SB@PO and SB@PN from sugarcane bagasse. The phosphate adsorption process uses a Box-Behnken design (BBD) to determine the optimum conditions for the adsorption process, with the output being a surface response curve between the influencing factors.

Materials and methods

We collected sugarcane bagasse from sugarcane juice vendors. The chemical reagents used in this study included acids, such as 65% nitric acid (HNO_3) from Merck, potassium dihydrogen phosphate (KH_2PO_4) from Merck, and phosphate standard solution (SRM from NIST) from Supelco®, $[\text{K}_3\text{Fe}(\text{CN})_6]$, and distilled water was used as the solvent in each solution.

Sugarcane bagasse waste was pyrolyzed under oxygen and N_2 atmosphere to produce SB@PO (oxygen) and SB@PN (nitrogen), which were used as adsorbents for phosphate adsorption. TGA, FTIR, XRD, and FESEM-EDX characterization were performed to determine the characteristics of SB@PO and SB@PN. Phosphate adsorption optimization was carried out using non-classical BBD and RSM approaches, followed by isothermal and kinetic studies. Phosphate adsorption concentration was measured using the differential pulse voltammetry (DPV) method.

Synthesis SB@PO and SB@PN from sugarcane bagasse

The initial stage involved washing and drying the bagasse obtained from sugarcane juice sellers. After drying, the bagasse was ground into powder with a particle size of < 100 mesh. The bagasse powder was pyrolyzed with vacuum furnace tube in an N₂ atmosphere at 400 °C for 6 h for SB@PN and in an oxygen atmosphere at 500 °C for 7.5 h for SB@PO with furnace. Each pyrolysis process with N₂ and oxygen atmosphere with a heating rate of 10 °C/min. After pyrolysis, SB@PO was pretreated at a 15 min washing process with 65% HNO₃ solution under constant stirring at room temperature (25 °C and 1 atm) to remove carbon and other impurities [24].

Characterization

Bagasse powder was first characterized by TGA with oxygen and nitrogen atmospheres to determine the decomposition time of the material. SB@PO and SB@PN were characterized by XRD, FTIR, FESEM-EDX, and N₂ adsorption-desorption to analyze the diffraction pattern, functional groups, shape, and surface morphology, and surface area of SB@PO and SB@PN. The results of phosphate adsorption optimization with SB@PO and SB@PN were characterized by FTIR to

determine the functional groups present before and after adsorption. Differential Pulse Voltammetry (DPV) was used to determine the performance of phosphate adsorption.

Phosphate ion adsorption

The adsorption of phosphate ions on SB@PO was optimized using parameters including contact time of 5, 15, and 30 min, adsorbent mass of 0.015, 0.02, and 0.025 g, and initial concentration of 1.2; 1.4; and 1.6 M in 25 mL of KH₂PO₄ solution. while on SB@PN with parameters including contact time of 30, 60, and 90 min, adsorbent mass of 0.05, 0.15, and 0.25 g, and initial concentration of 0.6; 0.8; and 1 M in 25 mL of KH₂PO₄ solution. Illustrate for adsorption of phosphate process shown in **Figure 1**. The removal percentage was calculated using Eq. (1).

$$Removal(\%) = 100 \times \frac{(C_o - C_e)}{C_o} \quad (1)$$

where *C_o* and *C_e* are the initial and equilibrium KH₂PO₄ concentrations (M), respectively. The initial (*C_o*) and the equilibrium (*C_e*) concentrations can be determined using a calibration curve of the KH₂PO₄ standard solution.

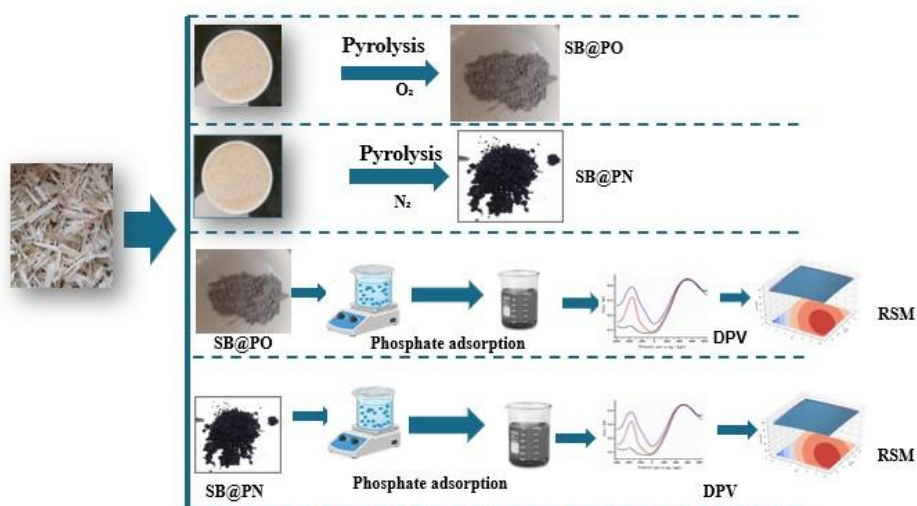


Figure 1 Illustrate for adsorption of phosphate process.

Experimental design for optimization

Response Surface Methodology (RSM) with Box-Behnken Design (BBD) was used to optimize phosphate ion adsorption. RSM is used to display the output of the

optimization process, while BBD is used to vary the input in the experimental design. BBD design, regression analysis, and response surface diagrams were performed using Python software. BBD requires less

experimentation compared to central composite design (CCD), thereby reducing chemical consumption during the optimization process. Optimization of phosphate ion adsorption using BBD with 3 factors and 3 levels requires 15 input variations. Three independent factors, namely adsorbent mass (X_1), contact time (X_2) and initial concentration (X_3), were examined at high (+1),

medium (0) and low (−1) values, respectively, as summarized in **Tables 1** and **2** RSM displays the optimization of factors influencing the phosphate ion with SB@PO and SB@PN, considering the response (%removal) and the relationship between response and factors.

Table 1 Box-behnken design for the phosphate ion adsorption with SB@PO.

Variables	Level		
	−1	0	+1
Adsorbent mass (g) (X_1)	0.015	0.02	0.025
Contact time (min) (X_2)	5	15	30
Initial concentration (M) (X_3)	1.2	1.4	1.6

Table 2 Box-behnken design for the phosphate ion adsorption with SB@PN.

Variables	Level		
	−1	0	+1
Adsorbent mass (g) (X_1)	0.05	0.15	0.25
Contact time (min) (X_2)	30	60	90
Initial concentration (M) (X_3)	0.6	0.8	1

Apparatus and electrochemical test procedure

A 3-electrode configuration was implemented in an electrochemical cell consisting of graphite as the working electrode, Ag/AgCl containing KCl as the reference electrode, and platinum wire ($T = 1$ mm) as the counter electrode. An aqueous solution of potassium ferric/ferrocyanide [$\text{Fe}(\text{CN})_6^{3-/4-}$] (5 mM) was prepared from acetate solution (0.1 M) and poured into the electrochemical cell equipped with 3 electrodes. The calibration curve of the potassium dihydrogen phosphate (KH_2PO_4) solution was tested using differential pulse voltammetry (DPV) from 1,000 to −1,000 mV at a scan rate of 100 mVs^{-1} and a current input of 20 mA. All electrochemical measurements, including differential pulse voltammetry (DPV), were performed using a computer-controlled potentiostat, an eDAQ model ER466 electrochemical analyzer, and EChem software (ES260) (eDAQ Pty Ltd, Australia).

Study isotherm and kinetics adsorption

The adsorption isotherm test was carried out using the batch equilibrium method. On SB@PO adsorbent by weighing 0.02 g at 20 min in 25 mL of aqueous solution with phosphate concentration. Samples were taken at

concentrations of 1, 1.2, 1.4, 1.6 and 1.8 M, respectively. On SB@PN adsorbent by weighing 0.15 g in 25 mL at 66 min in 25 mL of aqueous solution with phosphate concentration. Samples were taken at concentrations of 0.2, 0.4, 0.6, 0.8 and 1 M, respectively. and the concentration of phosphorus in water in the filtrate was measured after filtration. The phosphorus adsorption capacity of SB@PO and SB@PN was calculated, and the adsorption isotherm curves were plotted. The adsorption isotherm equations were fitted.

The adsorption kinetics test was carried out using the batch equilibrium method. In SB@PO adsorbent by weighing 0.02 g in 25 mL of aqueous solution with a phosphate concentration in water of 1.4 M. Samples were taken at 5, 10, 20, 30 and 40 min, respectively. In SB@PN adsorbent by weighing 0.15 g in 25 mL of aqueous solution with a phosphate concentration in water of 0.6 M. Samples were taken at 20, 35, 50, 65 and 80 min, respectively, and the phosphorus concentration in water in the filtrate was measured after filtration. The phosphorus adsorption capacity of SB@PO and SB@PN was calculated, and the adsorption kinetics curve was plotted. The adsorption kinetics equation was fitted.

Models for adsorption capacity, isotherm, and kinetics parameters.

$$Q = (C_0 - C) \div M \times V \quad (2)$$

In the above equation of adsorption capacity: Q is the adsorption amount (mg/g); C_0 is the initial mass concentration of the phosphate (mg/L); C is the end mass concentration of the phosphate (mg/L); V is the volume of the solution (L); M is the amount of adsorption substrate added (g); M_r is the molecular of phosphate ($\text{g} \cdot \text{mol}^{-1}$).

Adsorption isotherm equation

Langmuir equation

$$C_e/q_e = C_e/q_m + 1/(q_m \times K_L) \quad (3)$$

Freundlich equation

$$\ln q_e = (1 + n) \ln C_e + \ln k_F \quad (4)$$

Temkin equation

$$q_e = B \ln K_T + B \ln C_e \quad (5)$$

Dubinin-radushkevich equation

$$\varepsilon = R T \ln \left[\frac{1}{1 + C_e} \right] \quad (6)$$

where, C_e is the adsorption equilibrium solution concentration (mg/L), q_e denotes the adsorption amount (mg/g), q_m is the maximum adsorption amount (mg/g), and K_L , K_F , K_T are the Langmuir, Freundlich, and Temkin's adsorption constants, respectively. Where R is the universal gas constant which is 8.314 J/mol K and T is the temperature during adsorption (K).

Adsorption kinetic modelling

Pseudo-first-order equations:

$$\ln(q_e - q_t) = \ln q_{e1} - k_1 t / 2.303 \quad (7)$$

Pseudo-second-order equations

$$t/q_t = 1/k_2 q_e^2 + t/q_e \quad (8)$$

where, q_t is the adsorption amount at time t (mg/kg); t is the reaction time (s); a , k are the model parameters and q_e is the maximum adsorption amount (mg/g).

Results and discussion

Characterization

The physical appearance of Sugarcane Bagasse Pyrolysis Oxygen (SB@PO) and Sugarcane Bagasse Pyrolysis Nitrogen (SB@PN) is shown in **Figure 2**. Initially, the sugarcane bagasse powder looks like a light brown powder. Because sugarcane bagasse contains lignin, it makes the bagasse powder light brown. Lignin itself is a major component in plant cells that has a complex chemical structure and contains aromatic groups. When lignin is exposed to light, especially UV light, the light energy breaks the chemical bonds in lignin and produces free radicals that cause the lignin photodegradation process, thus giving plants a light brown color. After oxygen pyrolysis and HNO_3 pretreatment, the color changes to ash white, indicating conversion to SB@PO, ash white due to the oxidation and decomposition of organic compounds such as cellulose, hemicellulose, and lignin, leaving behind an inorganic residue rich in silica (SiO_2). Pyrolysis in an oxygen atmosphere removes other components such as carbon, hydrogen, and oxygen. After nitrogen pyrolysis, the color changes to black powder, indicating conversion to SB@PN. Organic components in bagasse, such as cellulose, hemicellulose, and lignin, decompose into carbon and other gaseous compounds such as CO , CO_2 , and H_2O . The resulting carbon cannot burn in the absence of oxygen and remains stable, remaining in solid form and giving it a black color. The decomposition of organic compounds causes this color change during the pyrolysis process, which produces ash white material rich in silica (SB@PO) and black material rich in carbon (SB@PN) [25].

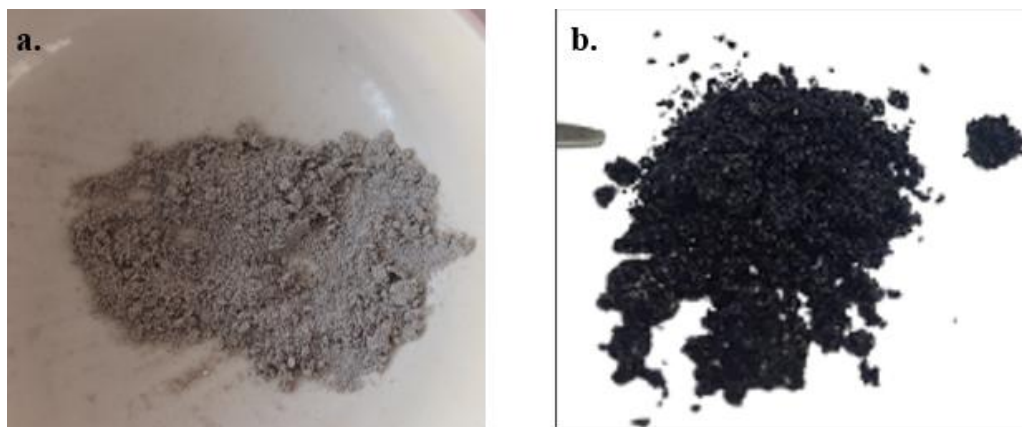


Figure 2 (a) SB@PO and (b) SB@PN are the results of pyrolysis of sugarcane bagasse.

Thermogravimetric analysis (TGA)

The sugarcane bagasse powder material was characterized by TGA (TG/DTA Hitachi STA7300, Germany) to determine the temperature and time of decomposition. In this case, TGA was determined using N₂ (SB@PN) and oxygen (SB@PO) atmospheres. The characterization results are shown in **Figure 3** TGA and DTA of SB@PO and SB@PN. Based on **Figure 3** shows the decomposition temperature of SB@PO and SB@PN materials. The first decomposition at a temperature of 100 - 200 °C. This indicates that at this temperature, decomposition of water and hemicellulose occurs. **Figure 3** shows that water decomposes at a temperature of 100 °C and hemicellulose decomposes at a temperature of 200 °C, which begins to decompose and releases volatile gases with %TG of 15%. At a

temperature of 350 °C, SB@PO decomposes faster than SB@PN and shows the decomposition of cellulose and lignin with %TG of 65%. In SB@PN, the material only decomposes by 80% and leaves carbon residue because in the pyrolysis process with nitrogen atmosphere there is no oxygen available to oxidize carbon to CO₂, leaving a carbon residue with a stable thermal structure and not easily decomposed at high temperatures up to 1,000 °C. In the N₂ pyrolysis process, amorphous carbon is obtained [26]. While in SB@PO, there is still decomposition at a temperature of 480 °C, which shows the decomposition of lignin and organic compounds. So, based on the TGA characterization for the SB@PN pyrolysis method using a temperature of 400 °C for 6 h, SB@PO using a temperature of 500 °C for 7.5 h [10].

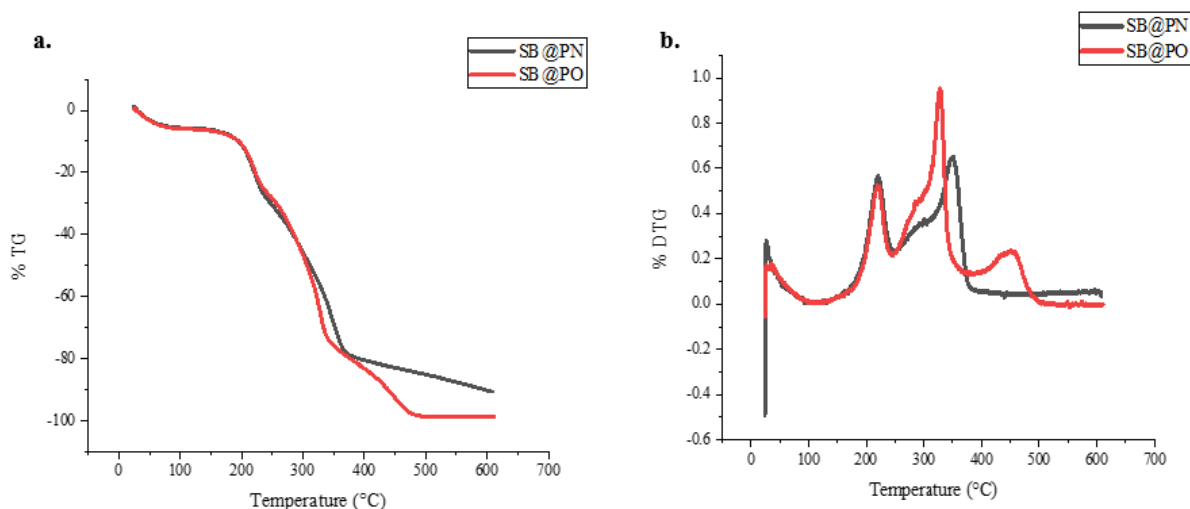


Figure 3 Thermogram of sugarcane bagasse; (a) TGA and (b) DTG of SB@PO and SB@PN from sugarcane bagasse.

According to research conducted by Torres *et al.* [27], at pyrolysis temperatures in an N₂ atmosphere, the carbon content increases with increasing temperature associated with the decomposition process of organic components such as cellulose, hemicellulose and lignin and other gases will decompose faster with increasing temperature to a certain point thereby increasing carbon content. This contrasts with pyrolysis in an oxygen atmosphere, where increasing temperatures cause the carbon to become ash and fly, leaving behind a higher silica content [6].

X-ray Diffractogram (XRD)

Sugarcane bagasse that has been pyrolyzed into SB@PO and SB@PN was characterized by XRD (Rigaku) with an angle of 2θ 5° - 90°. The results of the XRD characterization are shown in **Figure 4**. **Figure**

4(a) shows the diffractogram of SB@PO showing a peak band 2θ in the 20°, 30°, and 38° regions, which indicates cristobalite silica. Meanwhile, **Figure 4(b)** shows the diffractogram of SB@PN showing a broad peak band 2θ in the area between 15°, 22°, 30°, 35°, and 37°, representing amorphous silica cristobalite and carbon because this process does not have oxygen that oxidizes carbon to CO₂ by inhibiting the carbon crystallization process by filling the pores and reducing the mobility of carbon atoms so that the carbon formed cannot form regular crystals [4]. This is in accordance with previous research and data processing using Crystal Impact Match. Based on **Figure 4**, it shows that SB@PO shows a crystalline peak of silica cristobalite, while SB@PN shows an amorphous peak of carbon and silica cristobalite.

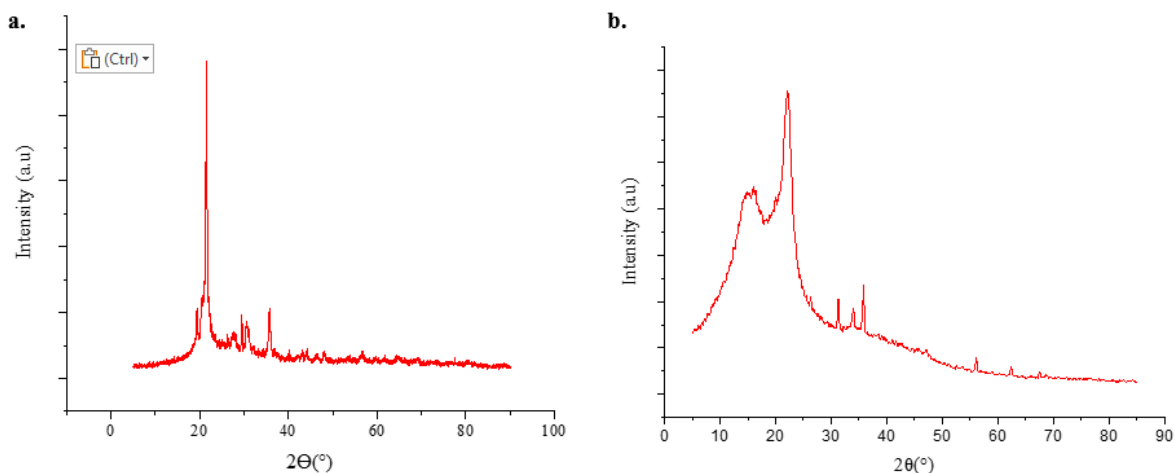


Figure 4 Diffractogram of sugarcane bagasse pyrolysis results (a) SB@PO and (b) SB@PN.

Fourier Transform Infrared (FTIR)

Sugarcane bagasse that has been pyrolyzed into SB@PO and SB@PN was characterized by an ATR-FTIR analyzer (Agilent Cary 630). Analysis of functional groups in SB@PO and SB@PN from bagasse was carried out using FTIR, as shown in **Figure 5**. **Figure 5(a)** shows that SB@PO has functional groups in the 1,000 - 1,100 cm⁻¹ region, which is Si-O-Si stretching, and in the 750 cm⁻¹ regions, which is Si-OH Asymmetry so from the figure it is concluded that

SB@PO is indicated to contain high silica content. **Figure 5(b)** shows that SB@PN has functional groups in the 3,225 cm⁻¹ regions, which shows -OH stretching vibrations, peaks in the 1,630 - 1,680 cm⁻¹ region indicate C=O functional groups. In the 1,000 - 1,100 cm⁻¹ regions shows Si-O-Si stretching vibrations. This is in accordance with research conducted by Ni'mah *et al.* [17]. Based on **Figure 5**, it can be concluded that SB@PO is indicated to contain high silica, while SB@PN is indicated to contain high carbon and silica.

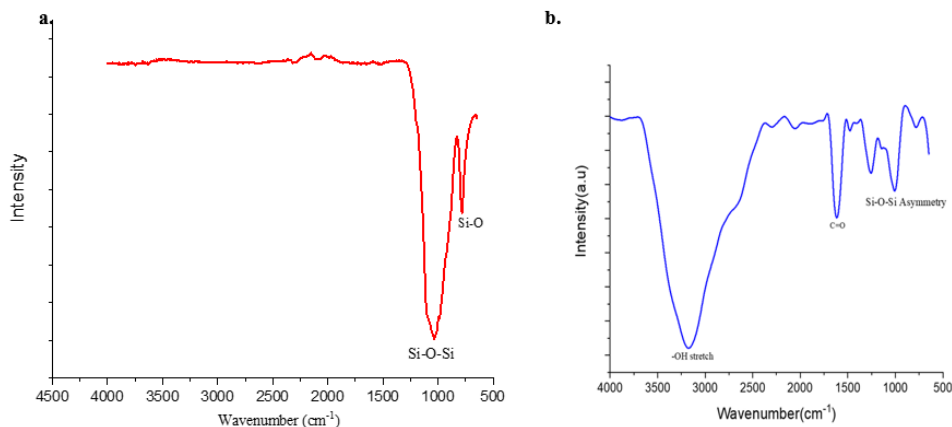


Figure 5 Spectra IR of sugarcane bagasse pyrolysis results (a) SB@PO and (b) SB@PN.

Field Emission Scanning Electron Microscope - Energy Dispersive X-ray Spectroscopy (FESEM-EDX)

The morphology of SB@PO and SB@PN was analyzed using FESEM-EDX (Hitachi Regulus 8220) as shown in **Figure 6** for SB@PO and **Figure 7** for SB@PN. In **Figure 6**, the FESEM image of SB@PO from sugarcane bagasse at magnifications of 15k×, 25k×, 50k×, 60k× and 70k× reveals the presence of small, round cavities on the surface, characterized by an irregular surface with a spherical shape. Additionally,

the morphology of SB@PO appears irregular because the surface of the material is oxidized to form an irregular structure and make the surface rough and uneven. The oxidation reaction occurs because oxygen reacts with components such as cellulose and lignin to form an irregular structure, exhibiting nanometer-sized particles. This is clarified by EDX in **Figure 6** (f and g), showing that SB@PO has the highest element content, namely Si (30.8%) and O (53.5%). This clarifies that SB@PO has a high silica content.

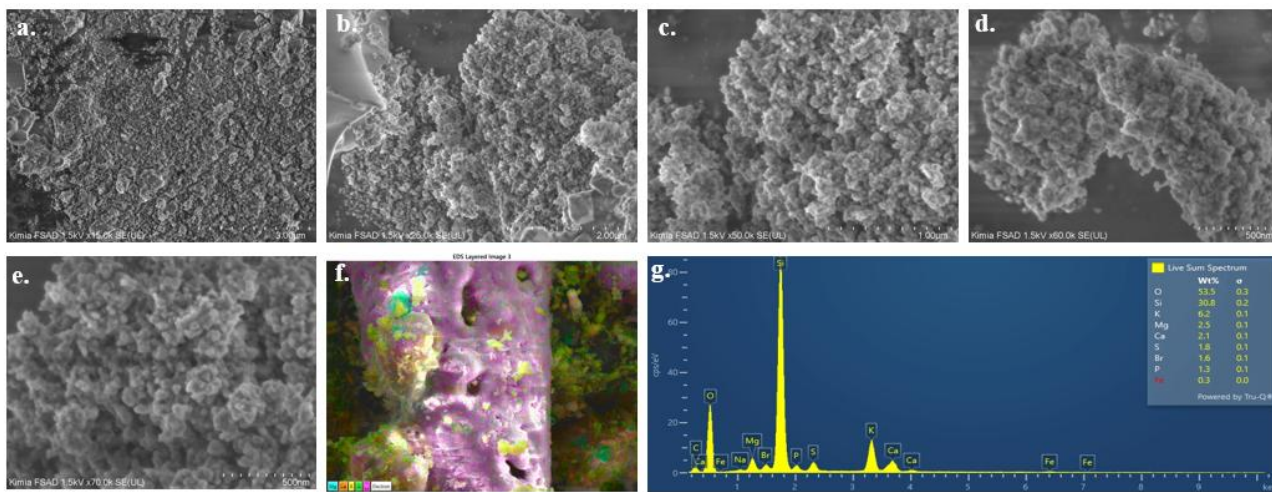


Figure 6 FESEM image with magnification of (a) 15k×, (b) 25k×, (c) 50k×, (d) 60k×, (e) 70kx, (f) and (g) EDX image of SB@PO from sugarcane bagasse.

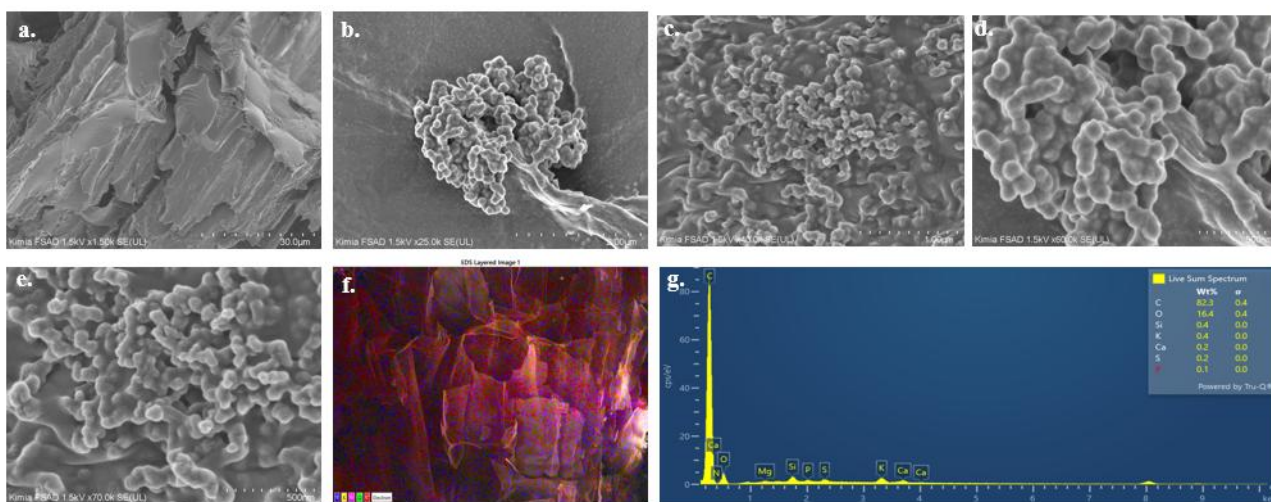


Figure 7 FESEM image with magnification of (a) 1.5k×, (b) 25k×, (c) 40k×, (d) 60k×, (e) 70k×, (f) and (g) EDX image of SB@PN from sugarcane bagasse.

In **Figure 7**, the FESEM image of SB@PN from sugarcane bagasse at magnifications of 1.5k×, 25k×, 40k×, 60k×, and 70k× shows the presence of small, round cavities on the surface with an irregular surface with a spherical shape. In addition, the morphology of SB@PN also appears irregular and shows nanometer-sized particles. This is clarified by EDX in **Figure 6** (f and g) showing that SB@PN has the highest element content, namely C (82.3%), Si (0.4%) and O (16.4%). This clarifies that SB@PN has a high carbon and silica content. The pyrolysis process with nitrogen atmosphere (SB@PN) there is no oxygen gas available to oxidize carbon to CO₂, leaving a carbon residue with a stable thermal structure and is not easily decomposed at high temperatures up to 1,000 °C. Thus producing a material

with a high carbon content. In this case, it is in accordance with research by Sarkar *et al.* [5] where sugarcane bagasse contains SiO, CaO, K₂O, and Fe₂O₃ [28].

Adsorption-desorption N₂

The surface area and pore diameter distribution of SB@PO and SB@PN were characterized by N₂ adsorption-desorption using the multi-point BET isotherm method. The specific pore surface area is an important parameter in determining the quality of the adsorbent. This is because the pore surface area affects the adsorption capacity of the adsorbent. The larger the pore surface area, the greater the adsorption capacity. Pore size distribution is also a parameter in the characterization study.

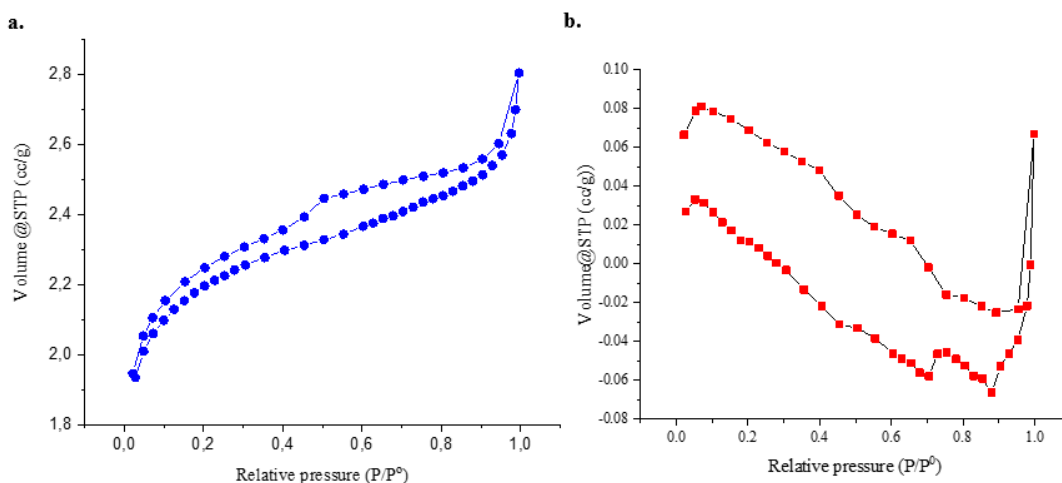
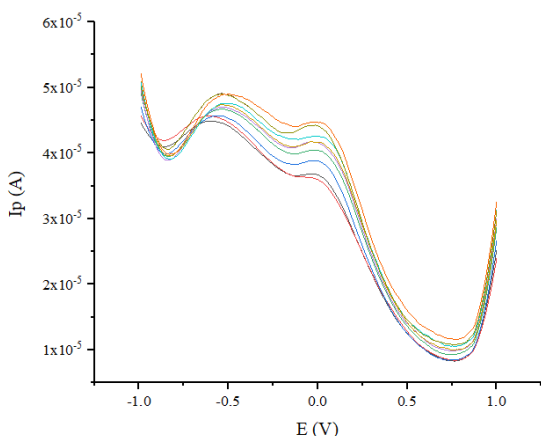


Figure 8 N₂ adsorption-desorption isotherm of (a) SB@PO and (b) SB@PN.

Figure 8 shows the adsorption-desorption N₂ of SB@PO (**Figure 8(a)**) and SB@PN (**Figure 8(b)**), where in SB@PO obtained a specific surface area of 236.971 m²/g with pore radius of 1.92 nm, and an isotherm type IV with a hysteresis loop, which explains that the material is mesoporous, while in SB@PN obtained a specific surface area of 0.139 m²/g with pore radius of 236.05 nm and the isotherm type is not defined. This is due to the large hysteresis loop because the surface conditions of the material change during the adsorption and desorption processes, which is contrary to the assumption of the BET theory, which assumes a fixed surface so that the adsorption and desorption curves do not meet each other, showing differences in behavior when the gas is absorbed and released from the surface of the material [29].



Study adsorption

Calibration curve

Determination of the calibration curve with a concentration of 0.1 to 1M. Each concentration was measured by Differential Pulse Voltammetry (DPV), and the peak current (Ip) was obtained, which was then plotted into a graph to obtain a calibration curve with a correlation coefficient (R²) of 0.9972 where when the R² value approaches 1 it indicating that there is an accurate and precise linear relationship between the predicted value and the test value. The calibration curve is shown in **Figure 9**, which is plotted in the Differential Pulse Voltammetry curve (**Figure 9(a)**) and the graph plot (**Figure 9(b)**) [30].

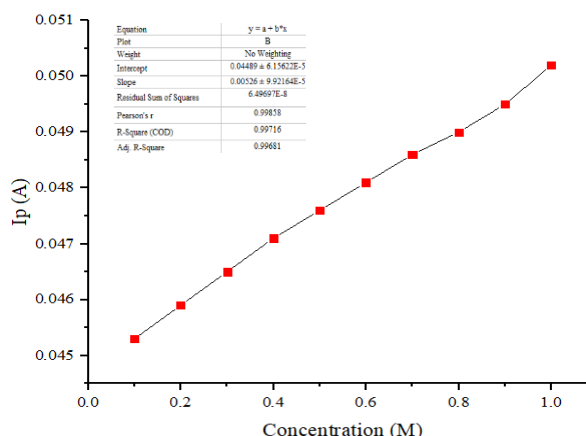


Figure 9 Calibration curve KH₂PO₄ 0.1 to 1 M.

Optimization of phosphate ion adsorption

Box-Behnken design (BBD) was applied for maximizing phosphate ion removal at SB@PO and SB@PN, the outcome of which is explained at **Table 3** for SB@PO and **Table 4** for SB@PN. Of the 15 experiments carried out, BBD optimization was involved for the perfection of input variables at order to maximize phosphate ion removal. to relate the experimental input variables for phosphate ion removal, multiple linear regression was used, like shown at Eq. (9) for SB@PO and Eq. (10) for SB@PN, Z represents the predicted response, and X₁, X₂, and X₃ are the coded values of the input variables.

$$Z = -4.016 + 59.325X_1 + 1.367X_2 + 59.892X_3 - 340.667X_1^2 - 0.109X_1X_2 + 58.875X_1X_3 - 0.007X_2^2 - 0.508X_2X_3 - 30.354X_3^2 \tag{9}$$

$$Z = -354.379 + 10738.216X_1 + 0.199X_2 + 481.181X_3 - 176483.333X_1^2 - 13.423X_1X_2 - 2350X_1X_3 - 0.029X_2^2 + 0.919X_2X_3 - 160.365X_3^2 \tag{10}$$

The data at the percentage removal were statistically analyzed and presented at **Table 3** and **Table 4**. Based on these results, the highest percentage removal of phosphate ion from the adsorption process utilizing SB@PO was achieved under the conditions of an adsorbent mass of 0.02 g, contact time of 20 min, and an initial concentration of 1.4 M, by a phosphate ion removal percentage of 95.97%. Removal of phosphate

ion from the adsorption process utilizing SB@PN was achieved under the conditions of an adsorbent mass of 0.15 g, contact time of 66 min, and an initial

concentration of 0.6 M, by a phosphate ion removal percentage of 65.73%.

Table 3 Box Behnken experimental design with independent variables for SB@PO.

Run no.	Coded variables levels			Removal percentage	
	X ₁	X ₂	X ₃	Experiment	Predicted
0	-1	-1	0	80.82	82.66
1	1	-1	0	86.30	85.88
2	-1	1	0	89.04	89.09
3	1	1	0	90.41	88.95
4	-1	0	-1	81.25	81.07
5	1	0	-1	85.94	87.65
6	-1	0	1	87.06	85.35
7	1	0	1	82.35	82.53
8	0	-1	-1	85.94	84.31
9	0	1	-1	84.38	84.47
10	0	-1	1	80.00	80.21
11	0	1	1	88.24	89.56
12	0	0	0	95.89	94.98
13	0	0	0	93.15	94.98
14	0	0	0	95.89	94.98

Table 4 Box Behnken experimental design with independent variables for SB@PN.

Run no.	Coded variables levels			Removal percentage	
	X ₁	X ₂	X ₃	Experiment	Predicted
0	-1	-1	0	53.95	51.25
1	1	-1	0	51.32	51.44
2	-1	1	0	57.89	57.77
3	1	1	0	53.95	56.65
4	-1	0	-1	60.00	62.88
5	1	0	-1	60.00	60.06
6	-1	0	1	56.47	56.41
7	1	0	1	61.18	58.30
8	0	-1	-1	52.73	52.55
9	0	1	-1	67.27	64.51
10	0	-1	1	51.76	54.52
11	0	1	1	54.12	54.30
12	0	0	0	63.16	64.03
13	0	0	0	64.47	64.03
14	0	0	0	64.47	64.03

The correlation coefficient (R²) of 0.942 is shown at the regression analysis for Eq. (9) for SB@PO and correlation coefficient (R²) of 0.873 is shown at the regression analysis for Eq. (10) for SB@PN among the

input variables and the removal of phosphate ion has a strong relationship. To assess the quality of the proposed model, the R² value by a value close for 1 shows higher prediction accuracy. The *p*-value tests the null

hypothesis for obtaining information about the correlation between the response and the independent variable. The significance of the design is indicated by a p -value below 0.05. The p -value (Prob F-static) was 0.0129 at the case of phosphate ion adsorption with SB@PO (See **Table S1**) and 0.0771 at the case ion phosphate adsorption with SB@PN (See **Table S2**) showing that the independent variables (adsorbent mass, contact time, and initial solvent concentration) had a significant correlation with the percentage of removal response. The adsorption performance of the SB@PO adsorbent is superior to that of SB@PN. This is because

SB@PN has a small surface area and the adsorption optimization process is only able to produce a removal percentage of 65.73%.

The response surface shown as a 3D graph in **Figure 10** for SB@PO adsorbent and **Figure 11** for SB@PN adsorbent helps understand the relationship between the test factors and phosphate ion removal. This 3D graph is generated by plotting the percentage decrease on the Z-axis against 2 test variables while keeping the other variable constant at level 0. Different color zones can be seen on the contour plot of the 3D graph.

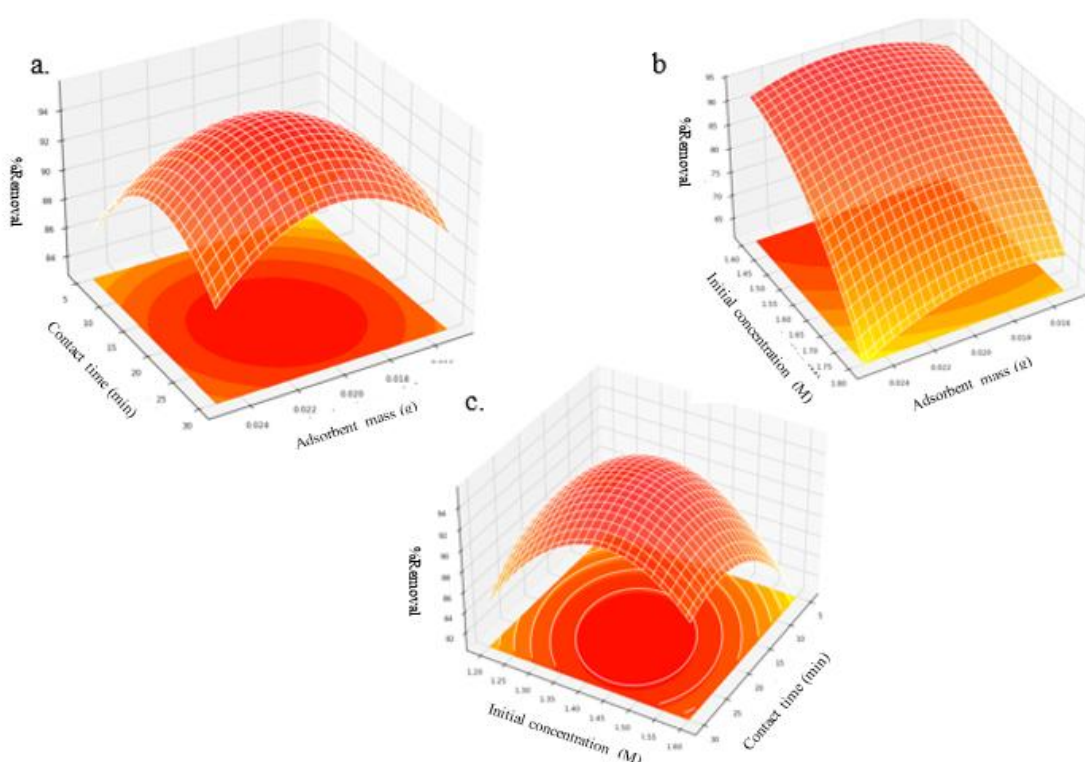


Figure 10 Response Surface (3-D) shows the effect of % removal phosphate adsorption with SB@PO to (a) contact time vs. adsorbent mass, (b) initial concentration vs. adsorbent mass, and (c) initial concentration vs. contact time.

Based on the 3D RSM curve in **Figure 10**, the optimum conditions for phosphate ion adsorption with SB@PO include an adsorbent mass of 0.02 g, a contact time of 20 min, and an initial concentration of 1.4 M, by a phosphate ion removal percentage of 95.97%. The 3D RSM curve in **Figure 11** shows the optimum conditions for phosphate ion adsorption with SB@PN including an adsorbent mass of 0.15 g, a contact time of 66 min, and an initial concentration of 0.6 M, by a phosphate ion removal percentage of 65.73% with error analysis shown in **Figure 12** and **Table 5** namely MAE (Mean

Absolute Error), MSE (Mean Squared Error), RMSE (Root Mean Squared Error), and residual plot analysis. Error analysis studies are conducted to identify model weaknesses, improve models, understand data, and evaluate performance by reducing errors and increasing accuracy so that the model is suitable for use. Based on study, it was shown that SB@PO has a smaller error than SB@PN, where the MAE, MSE, and RMSE values are closet to zero. Based on **Figure 12(a)**, it shows that the residual plot is slightly skewed towards the negative with high and narrow peak so that the drain is normally

distributed. Based on **Figure 12(b)**, the residual points appear more symmetrical and closer to the ideal bell shape, with peaks more centered around the 0 value (the

mean of the residuals). Based on its visual shape, SB@PO is more normally distributed than SB@PN.

Table 5 Study error analysis adsorption of phosphate with SB@PO and SB@PN adsorbent.

Type Adsorbent	Study Error Analysis		
	MAE	MSE	RMSE
SB@PO	0.96	1.4	1.18
SB@PN	1.27	3.18	1.78

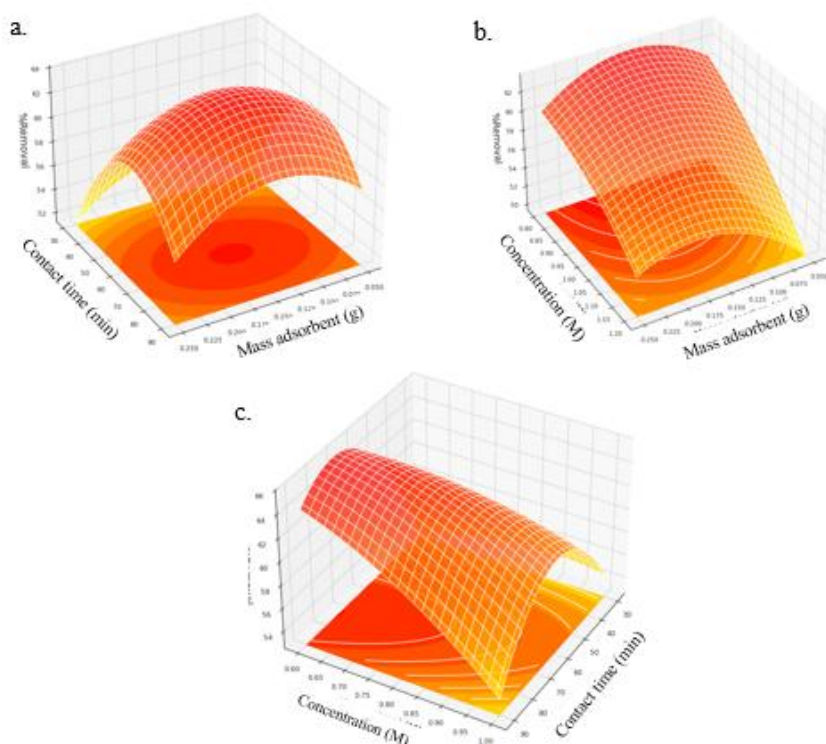


Figure 11 Response Surface (3-D) shows the effect of % removal phosphate adsorption with SB@PN to (a) contact time vs. adsorbent mass, (b) initial concentration vs. adsorbent mass, and (c) initial concentration vs. contact time.

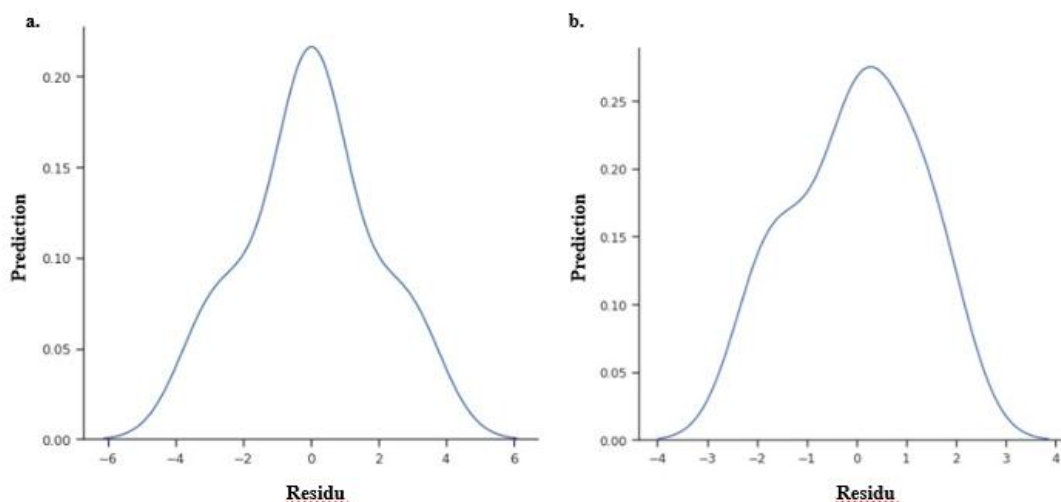


Figure 12 Plot analysis residual; (a) SB@PO and (b) SB@PN.

Adsorption isotherm models of phosphate at SB@PO and SB@PN

Table 6 summarizes the optimal data that was applied to create the adsorption isotherm model. The

phosphate adsorption regressions for Langmuir, Freundlich, Temkin, and Dubinin-Radushkevich, for SB@PO and SB@PN adsorbent.

Table 6 Examination of the Freundlich, Temkin, Dubinin-Radushkevich, Langmuir isotherm.

Parameter Isotherm		SB@PO	SB@PN
Langmuir	qm ($\text{mg}\cdot\text{g}^{-1}$)	43.48	0.236
	K_L ($\text{L}\cdot\text{mg}^{-1}$)	4,600	-2.12×10^5
	R^2	0.9985	0.4220
Freundlich	n	9.07	0.825
	K_F ($\text{mg}\cdot\text{g}^{-1}$)	8.64×10^{10}	3.09×10^{-4}
	R^2	0.9685	0.9653
Temkin	B_T ($\text{J}\cdot\text{mol}^{-1}$)	19394	13522
	K_T ($\text{L}\cdot\text{mg}^{-1}$)	0.285	$5.9-10^{-5}$
	R^2	0.9623	0.9726
Dubinin-Radushkevich	qm ($\text{mg}\cdot\text{g}^{-1}$)	14.926	2.2×10^{-4}
	β ($\text{mol}^2\cdot\text{J}^{-2}$)	0.222	1×10^7
	E ($\text{kJ}\cdot\text{mol}^{-1}$)	1.5	2.236
	R^2	0.7079	0.9769

The correlation coefficients for each isotherm design are shown at Table 6 shows that the adsorption with SB@PO data closely matched the Langmuir isotherm model, by the Langmuir isotherm showing the greatest correlation coefficient (R^2) at 0.9985. The maximum adsorption power (qm) of the Langmuir was found to be 43.48 mg/g. Adsorption of monolayer adsorption indicated adsorption occurs when adsorbate molecules attach to active sites on the surface of the adsorbent and form a single layer [31]. The adsorption data with SB@PN is in good agreement with the Dubinin-Radushkevich isotherm model which shows the largest correlation coefficient (R^2) of 0.9769. The adsorption of porous materials, especially microporous materials, is explained by this model. The multi-layered adsorption properties are indicated by the pore filling mechanism applied to the adsorption process. This was determined using the $E < 8$ kJ/mol (physisorption) and 8 - 16 kJ/mol (chemisorption) approaches, which obtained ($E = 2.236$ kJ/mol) so that the adsorption of

phosphate with SB@PN occurs by physisorption where adsorption occurs due to Van der Waals forces between the adsorbate molecules and the adsorbent surface [32].

Adsorption kinetics models of phosphate at SB@PO and SB@PN

The regression coefficient for SB@PO (Figure 13), namely Langmuir is 0.9985, and the calculated q_e values for various phosphate concentrations are in good agreement with the experimental results. The isotherm kinetics is close to pseudo-second order, namely the correlation coefficient value of 0.9992. This implies that chemisorption is the main mechanism, which means that the critical step in the adsorption process is the interaction between phosphate ions and the surface groups of the adsorbent. Higher initial phosphate concentrations result in an increase in the adsorption quantity at equilibrium, indicating a greater mass transfer driving force that allows more phosphate ions to reach the adsorbent surface quickly [33].

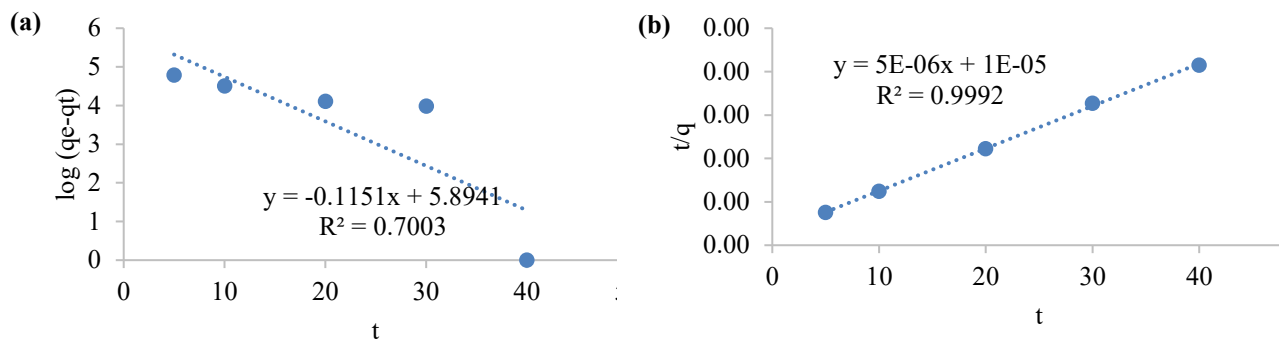


Figure 13 Adsorption kinetics of SB@PO adsorbent (a). pseudo-first-order, (b). pseudo-second-order.

The regression coefficient for SB@PN (**Figure 14**), namely Dubinin-Radushkevich, is 0.9769. The isotherm kinetics approaches pseudo-first order, namely the correlation coefficient value of 0.624. This implies

that physisorption is the main mechanism, which means that the critical stage in the adsorption process is the interaction between phosphate ions and the surface groups of the adsorbent [16].

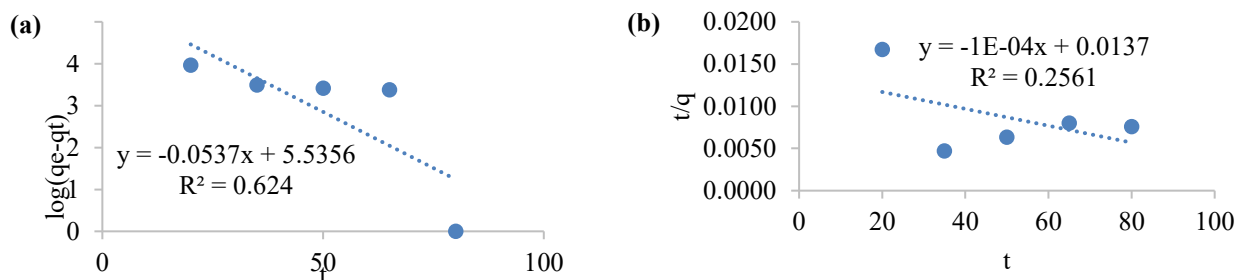


Figure 14 Adsorption kinetics of SB@PN adsorbent; (a) pseudo-first-order and (b) pseudo-second-order.

Comparative study

A comparison was made between the characterization and optimization of phosphate ion adsorption achieved in this study using 2 different adsorbents in the atmosphere in the pyrolysis method,

namely SB@PO and SB@PN adsorbents used for phosphate ion adsorption. The comparison of SB@PO and SB@PN derived from sugarcane bagasse used for phosphate ion adsorption is shown in **Table 7**.

Table 7 Comparative study on phosphate adsorption with SB@PO and SB@PN adsorbent.

Comparison	SB@PO	SB@PN
Material	Sugarcane bagasse	Sugarcane bagasse
Methods	Pyrolysis atmosfer O ₂	Pyrolysis Atmosfer N ₂
Equipment	Furnace	Vaccum furnace tube
Temperature (°C)	500	400
Time pyrolysis (h)	7.5	6
Characterization		
X-ray diffraction (XRD)	Silica cristobalite	Carbon, Silica Amorphous
FTIR	Si-O-Si stretching, Si-OH Asymmetry	OH stretching, CO bending, Si-O-Si Asymmetry
EDX	Si (30.8%) and O (53.5%)	C (82.3%), Si (0.4%) and O (16.4%)

Comparison	SB@PO	SB@PN
Specific surface area (m ² /g)	236.971	0.139
pore radius (nm)	1.92	236.05
Optimization of phosphate ion adsorption		
Contact time (min)	21	66
Mass of adsorbent (g)	0.02	0.15
Initial concentration (M)	1.4	0.6
Percentage removal (%)	95.97	65.75
Isotherm adsorption	Langmuir	Dubinin-radushkevich
Kinetics adsorption	pseudo-second-order	pseudo-first-order
Adsorption capacity (mg/g)	43.48	2.2×10 ⁻⁴

Validation method

Validation methods are used to ensure that an analytical method or process is suitable for its intended purpose and is reliable. In validation, several aspects that need to be discussed include accuracy, precision, detection limit, quantification limit, and robustness. Validation is conducted to ensure that the method

produces accurate and reliable data. Method validation in this study used a phosphate solution of KH₂PO₄ and standard reference material (SRM) for phosphate analysis. Validation method to determine the phosphate measurement process using the differential pulse voltammetry (DPV) method. The validation process obtained the results shown in **Table 8**.

Table 8 Summary of method validation.

Validation Parameters	Phosphate	SRM Phosphate
Coefficient Determination (R ²)	0.997	0.9983
Regression equation (y)	$y = 0.0053x + 0.044$	$y = 0.00002x + 0.0006$
Slope (b)	0.0053	0.00002
Intercept (a)	0.044	0.0006
Limit of detection	0.0057	0
Limit of quantification	0.0189	0
Precision (%RSD NMT 2%)	1.41	0
Accuracy	Unbiased	unbiased
Robustness	Robust	Robust

Conclusions

This study showed that the pyrolysis process plays a significant role in determining the physicochemical properties and phosphate adsorption performance of the adsorbent derived from sugarcane bagasse. Pyrolysis under O₂ atmosphere produced nanometer size and material content in the form of Si (30.8%) and O (53.5%) with a significantly higher surface area of 236,971 m²/g, resulting in superior phosphate adsorption compared to the carbon-dominated adsorbent obtained under N₂ atmosphere while the

characterization of SB@PN showed carbon and amorphous silica, nanometer size and material content in the form of C (82.3%), Si (0.4%) and O (16.4%) with a specific surface area of 0.139 m²/g. Optimization of phosphate adsorption with RSM-BBD showed optimum conditions for SB@PO including adsorbent mass of 0.02 g, a contact time of 21 min, and an initial concentration of 1.4 M with a percentage removal and adsorption capacity of 95.97%, 43.48 mg/g with Langmuir isotherm rate and pseudo-second-order kinetics, while SB@PN was optimum an adsorbent

mass of 0.15 g, a contact time of 66 min, and an initial concentration of 0.6 M with a percentage removal and adsorption capacity of 65.75% and 2.2×10^{-4} mg/g with Dubinin-Radushkevich isotherm rate and pseudo-first-order kinetics. This study shows that SB@PO shows superior adsorption performance compared to SB@PN.

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Declaration of generative AI in scientific writing

The authors acknowledge the use of generative AI tools (e.g., QuillBot and ChatGPT by OpenAI) in the preparation of this manuscript, specifically for language editing and grammar correction. No content generation or data interpretation was performed by AI. The authors take full responsibility for the content and conclusions of this work.

CRedit author statement

Yatim Lailun Ni'mah: Conceptualization; Methodology; Supervision; Validation. **Nabila Eka Yuningsih:** Data curation; Writing - Original draft preparation; Reviewing and Editing. **Suprpto Suprpto:** Visualization; Investigation; Software; Supervision.

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Supplementary data

Table S1 OLS regression adsorption of phosphate at SB@PO.

OLS Regression Results						
Dep. Variable:	y		R-squared:	0.942		
Model:	OLS		Adj. R-squared:	0.838		
Method:	Least Squares		F-statistic:	9.065		
Date:	Sun, 28 Sep 2025		Prob (F-statistic):	0.0129		
Time:	05:29:38		Log-Likelihood:	-23.825		
No. Observations:	15		AIC:	67.65		
Df Residuals:	5		BIC:	74.73		
Df Model:	9					
Covariance Type:	nonrobust					
	coef	std err	T	P > t 	[0.025	0.975]
Const	-354.38	63.84	-5.551	0.003	-518.5	-190.3
x1	1.07e + 04	2252	4.768	0.005	4948	1.65e + 04
x2	0.199	0.707	0.281	0.790	-1.62	2.016
x3	481.88	77.87	6.179	0.002	280.99	681.36
x4	-1.7e + 05	4.27e + 04	-4.132	0.009	-2.8e + 05	-6.7e + 04
x5	-13.42	16.25	-0.826	0.446	-55.20	28.36
x6	-2350	0.007	-2.291	0.071	-4987	287.11
x7	-0.029	0.406	-4.081	0.010	-0.048	-0.011
x8	-0.92	0.406	2.261	0.073	-0.126	1.963
x9	-160.36	26.69	-6.007	0.002	-228.98	-91.75
Omnibus:	1.471		Durbin-Watson:	2.637		
Prob(Omnibus):	0.479		Jarque-Bera (JB):	0.904		
Skew:	-0.224		Prob(JB):	0.636		
Kurtosis:	1.884		Cond. No.	3.96E + 07		

Table S2 OLS regression adsorption of phosphate at SB@PN.

OLS Regression Results						
Dep. Variable:	y		R-squared:	0.873		
Model:	OLS		Adj. R-squared:	0.644		
Method:	Least Squares		F-statistic:	3.817		
Date:	Sun, 28 Sep 2025		Prob (F-statistic):	0.0771		
Time:	05:29:38		Log-Likelihood:	-29.961		
No. Observations:	15		AIC:	79.92		
Df Residuals:	5		BIC:	87.00		
Df Model:	9					
Covariance Type:	nonrobust					
	coef	std err	t	P > t 	[0.025	0.975]
const	-4.016	31.28	-0.128	0.903	-84.41	76.38
x1	59.33	84.94	0.698	0.516	-159.03	277.68
x2	1.37	0.309	4.420	0.007	0.572	2.162
x3	59.89	67.36	0.889	0.415	-113.253	233.04

OLS Regression Results						
x4	-340.67	160.75	-2.119	0.088	-753.881	72.55
x5	-0.11	0.515	-0.212	0.840	-1.433	1.214
x6	58.88	77.22	0.762	0.480	-139.63	277.38
x7	-0.0071	0.002	-3.950	0.011	-0.012	-0.002
x8	-0.51	0.257	-1.972	0.106	-1.169	0.154
x9	-30.35	40.19	-0.755	0.484	-133.66	-72.95
Omnibus:	1.019		Durbin-Watson:	1.788		
Prob(Omnibus):	0.990		Jarque-Bera (JB):	0.238		
Skew:	-0.006		Prob(JB):	0.888		
Kurtosis:	2.382		Cond. No.	1.04E + 06		
